

AN EXTENSION OF ORDER PRESERVING OPERATOR INEQUALITY

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Abstract. We discuss an order preserving operator inequality and also we transform it into log majorization.

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