

SOME INEQUALITIES FOR OPERATOR MEANS AND HADAMARD PRODUCT

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Abstract. We prove some general theorems which unify results on arithmetic-geometric mean and some other related matrix inequalities. As an application we obtain some results involving Hadamard product of matrices.

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