

A PRIORI ESTIMATES FOR ELLIPTIC EQUATIONS IN WEIGHTED SOBOLEV SPACES

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Abstract. In this paper we prove some a priori bounds for the solutions of the Dirichlet problem for elliptic equations with singular coefficients in weighted Sobolev spaces.

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