

WEIGHTED CRITERIA FOR ONE-SIDED POTENTIALS WITH PRODUCT KERNELS ON CONES OF DECREASING FUNCTIONS

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Abstract. Necessary and sufficient conditions governing two-weight estimates for one-sided potentials with multiple kernels and corresponding one-sided strong fractional maximal functions are established. The one-weight problem for the multiple Riemann–Liouville transform is also studied.

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