

## MERCER'S INEQUALITY AND TOTALLY MONOTONIC SEQUENCES

GRAHAME BENNETT

*Abstract.* A simple inequality of Mercer leads to some intriguing problems concerning moment sequences.

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