

## WEAK TYPE INEQUALITY FOR THE ONE-DIMENSIONAL DYADIC DERIVATIVE

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*Abstract.* It is shown that the maximal operator of the one-dimensional dyadic derivative of the dyadic integral is bounded from the dyadic Hardy space  $H_{1/2}$  to the space weak- $L_{1/2}$ .

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