

A LYAPUNOV–TYPE INEQUALITY FOR A TWO–TERM EVEN–ORDER DIFFERENTIAL EQUATION

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Abstract. In this note, a new inequality is obtained for a two-term even-order linear differential equation, which generalizes the well-known Lyapunov-type inequality for second order linear differential equations.

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