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POLAROID AND $p-*-$PARANORMAL OPERATORS

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Abstract. In this paper we define the $p-*-$ paranormal operators and we show some properties of this class of operators. We also prove that a $p-*-$paranormal operator is polaroid and we show a necessary and sufficient condition for the Riesz idempotent associated to a non-zero isolated point of the spectrum of a $p-*-$paranormal operator to be self-adjoint. Finally, we show that generalized a-Weyl's theorem holds for $p-*-$ paranormal operators and we present some finite operators.

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Paper MIA-16-41

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