

## SHEPHARD TYPE PROBLEMS FOR $L_p$ -CENTROID BODIES

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*Abstract.* Lutwak and Zhang proposed the notion of the  $L_p$ -centroid body. In this article, based on the definition of  $L_p$ -dual affine surface area, we research Shephard type problems for the  $L_p$ -centroid body

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