

ON WEIGHTED BERNSTEIN TYPE INEQUALITY IN GRAND VARIABLE EXPONENT LEBESGUE SPACES

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Abstract. In this paper a weighted Bernstein type inequality on derivatives of trigonometric polynomials is established in new function spaces unifying two nonstandard Banach function spaces, in particular, grand and variable exponent Lebesgue spaces.

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