

A GENERALIZATION OF MERCER'S RESULT ON CONVEX FUNCTIONS, II

MAREK NIEZGODA

Abstract. In this paper, we apply Jensen's inequality and two kinds of majorization for matrices in order to generalize some recent results on Mercer's inequality for convex functions.

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