

SMALL HANKEL OPERATORS ON DIRICHLET-TYPE SPACES AND APPLICATIONS

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Abstract. In this paper, we characterize the boundedness and compactness of small Hankel operators on Dirichlet-type spaces D_p .

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