

FRACTIONAL INTEGRALS ON B_σ -WEIGHTED MORREY SPACES

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Abstract. By using B_σ -weighted function spaces, we will investigate the weighted estimates of fractional integrals on B_σ -weighted Morrey spaces, which unify the weighted estimates of them on several function spaces.

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