

OPTIMAL EVALUATIONS FOR THE SÁNDOR–YANG MEAN BY POWER MEAN

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Abstract. In this paper, we present the best possible upper and lower bounds for the Sándor–Yang mean in terms of the power mean.

Mathematics subject classification (2010): 26E60.

Keywords and phrases: Power mean, Seiffert mean, arithmetic mean, quadratic mean, Sándor–Yang mean.

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