

JENSEN, HÖLDER, MINKOWSKI, JENSEN–STEFFENSEN AND SLATER–PEČARIĆ INEQUALITIES DERIVED THROUGH N -QUASICONVEXITY

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Abstract. Jensen, Hölder, Minkowski, Jensen-Steffensen and Slater-Pečarić type inequalities derived by the properties of γ -quasiconvex functions that we deal with here, can be seen as analog to these for superquadratic functions and refinements of these for convex functions.

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