

APPLICATIONS OF THE HERMITE–HADAMARD INEQUALITY

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Abstract. We show how the recent improvement of the Hermite–Hadamard inequality can be applied to some (not necessarily convex) planar figures and three-dimensional bodies satisfying some kind of regularity.

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