

## ESSENTIAL NORM OF THE DIFFERENCES OF COMPOSITION OPERATORS ON THE BLOCH SPACE

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*Abstract.* We provide some estimates for the essential norm of the differences of composition operators  $C_\varphi - C_\psi$  acting on the Bloch space by using pseudo-hyperbolic distance, Möbius transformation and  $\varphi^n - \psi^n$ .

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