

CHARACTERIZATIONS OF BOUNDEDNESS FOR GENERALIZED FRACTIONAL INTEGRALS ON MARTINGALE MORREY SPACES

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Abstract. On generalized martingale Morrey spaces we give necessary and sufficient conditions for the boundedness of generalized fractional integrals as martingale transforms.

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