

A NEW CHARACTERIZATION OF DIFFERENCES OF GENERALIZED WEIGHTED COMPOSITION OPERATORS FROM THE BLOCH SPACE INTO WEIGHTED-TYPE SPACES

QINGHUA HU AND XIANGLING ZHU

Abstract. In this paper, we give a new characterization for the boundedness and compactness of differences of generalized weighted composition operators from the Bloch space into weighted-type spaces. Moreover, we give some estimates for the essential norm of these operators.

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