

EMBEDDING GENERALIZED WIENER CLASSES INTO LIPSCHITZ SPACES

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Abstract. In this note, we give a necessary and sufficient condition for embedding the classes $\Lambda BV^{(p_n, 1, p)}$ into the generalized Lipschitz spaces H_q^ω ($1 \leq q < p \leq \infty$).

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