

## ON STEVIĆ–SHARMA TYPE OPERATOR FROM THE BESOV SPACES INTO THE WEIGHTED-TYPE SPACE $H_{\mu}^{\infty}$

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*Abstract.* We completely describe the boundedness and compactness of Stević-Sharma type operator  $T_{\psi_1, \psi_2, \varphi}$  from the Besov spaces  $B_p$  ( $1 < p < \infty$ ) into the weighted-type space  $H_{\mu}^{\infty}$  or the little weighted-type space  $H_{\mu, 0}^{\infty}$ .

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