

## CONTINUITY PROPERTIES OF $K$ -MIDCONVEX AND $K$ -MIDCONCAVE SET-VALUED MAPS

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*Abstract.* A recent result on the continuity of midconvex functionals upper bounded on a not null-finite set (see [2]) is extended to  $K$ -midconvex and  $K$ -midconcave set-valued maps.

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