

FURTHER IMPROVEMENT OF AN EXTENSION OF HÖLDER–TYPE INEQUALITY

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Abstract. In 1995 Pearce and Pečarić proved an extension of Hölder’s inequality. In this paper we extend their result in a measure theoretic sense and further improve it using log-convexity of related linear functionals. Moreover, we study the action of related linear functionals on families of exponentially convex functions.

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