

NOTE ON STRICHARTZ INEQUALITIES FOR THE WAVE EQUATION WITH POTENTIAL

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Abstract. We obtain Strichartz inequalities for the wave equation with potentials which behave like the inverse square potential $|x|^{-2}$ but might be not a radially symmetric function.

Mathematics subject classification (2010): 35B45, 35L05.

Keywords and phrases: Strichartz estimates, wave equation.

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