

ON MULTIVARIATE OSTROWSKI TYPE INEQUALITIES AND THEIR APPLICATIONS

VLADYSLAV BABENKO, YULIYA BABENKO AND OLEG KOVALENKO

Abstract. We prove sharp Ostrowski type inequality for multivariate Sobolev classes and apply it to the problem of optimal recovery of integrals.

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