

## POLYNOMIAL INEQUALITIES ON MEASURABLE SETS IN LORENTZ SPACES AND THEIR APPLICATIONS

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*Abstract.* In this short note, we study inequalities for algebraic polynomials on measurable sets in Lorentz spaces and discuss their applications to best approximation.

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