

WEIGHTED COMPOSITION OPERATORS FROM DIRICHLET-TYPE SPACES INTO STEVIĆ-TYPE SPACES

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Abstract. The boundedness and compactness of weighted composition operators from Dirichlet-type spaces into Stević-type spaces are investigated in this paper. Some estimates for the essential norm of weighted composition operators are also given.

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