

STABILITY ESTIMATES FOR A RADICAL FUNCTIONAL EQUATION WITH FIXED-POINT APPROACHES

DONGSEUNG KANG, HOEWOON KIM* AND BONGWOO LEE

Abstract. We investigate the stability problem of a radical functional equation using both Brzdęk fixed point theorem and fixed point alternative method.

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