

ON q -MONOTONICITY OF α -BERNSTEIN OPERATORS

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Abstract. In this paper we show that α -Bernstein operators preserve q -monotonicity of all orders. We investigate the tensor product of two such operators and show that it preserves (q, s) -box convexity. Some Raşa type inequalities for the α -Bernstein operators are also derived.

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