

## INEQUALITIES FOR TRIGONOMETRIC SUMS IN TWO VARIABLES

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*Abstract.* We prove sharp inequalities for the two-variable versions of the sum  $\sum_{k=1}^n \frac{\sin(kx)}{k}$ .

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