

MULTIDIMENSIONAL WEIGHTED PÓLYA–KNOPP INEQUALITIES WITH SHARP CONSTANTS

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Abstract. Some new Pólya–Knopp inequalities in two and higher dimensions with sharp constants are stated and proved. Furthermore, some new general weighted Pólya–Knopp type inequalities in n -dimension are proved and applied.

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