

REFINEMENTS OF BENNETT TYPE INEQUALITIES

J. A. OGUNTUASE*, L.-E. PERSSON AND E. O. ADELEKE

Abstract. In this paper we discuss, complement and improve some Bennett type inequalities. In particular, we prove a new refinement of a Bennett type inequality using superquadracity argument.

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