

AN INTERTWINED CAUCHY—SCHWARZ—TYPE INEQUALITY BASED ON A LAGRANGE—TYPE IDENTITY

IOSIF PINELIS

Abstract. Based on an apparently new Lagrange-type identity, a Cauchy–Schwarz-type inequality is proved. The mentioned identity is obtained by using certain “macro” variables; it is hoped that such a method can be used to prove or produce other identities and inequalities.

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