

ON L^p MARKOV TYPE INEQUALITY FOR SOME CUSPIDAL DOMAINS

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Abstract. The purpose of this paper is to study a Markov type inequality for algebraic polynomials in L^p norm on two-dimensional cuspidal domains.

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