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WEIGHTED ESTIMATES FOR A CLASS OF MATRIX OPERATORS

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Abstract. In this paper, we have obtained criteria for the fulfillment of weighted inequalities for the class of quasilinear discrete operators involving matrix kernels.

Mathematics subject classification (2020): 26D15, 26D20.
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