

DIRAC INEQUALITY FOR HIGHEST WEIGHT HARISH-CHANDRA MODULES II

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Abstract. Let G be a connected simply connected noncompact exceptional simple Lie group of Hermitian type. In this paper, we work with the Dirac inequality which is a very useful tool for the classification of unitary highest weight modules.

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