

EXTENSION FORMULAS AND NORM INEQUALITIES IN SOBOLEV HILBERT SPACES

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Abstract. In this note, we shall consider extension formulas and norm inequalities for some typical Sobolev Hilbert spaces. We see many related open problems.

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