

ON THE CALCULATIONS OF THE GENERALIZED VON NEUMANN–JORDAN CONSTANTS $C_{NJ}^{(p)}(L_r(\Omega, \Sigma, \mu))$ AND $\tilde{C}_{NJ}^{(p)}(L_r(\Omega, \Sigma, \mu))$

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Abstract. In this paper, we calculate $C_{NJ}^{(p)}(L_r(\Omega, \Sigma, \mu))$ and $\tilde{C}_{NJ}^{(p)}(L_r(\Omega, \Sigma, \mu))$, where (Ω, Σ, μ) is a measure space and $r > 1$.

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