

## COMMUTATORS, PINCHINGS, AND SPECTRAL VARIATION

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*Abstract.* The three topics of the title have been studied by several authors. The main aim of this note is to point out interesting connections between them.

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