

ON OPERATORS WITH LARGE SELF-COMMUTATORS

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Abstract. We study the "size" of self-commutator of Hilbert space operator. Different properties of operators, having large self-commutators are established. Possible values of the numerical radius of such operators are investigated. Two necessary and sufficient conditions of equality $\|A\| = 2w(A)$ are mentioned.

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