

## REDUCTION OPERATOR ALGEBRAS AND GENERALIZED SIMILARITY PROBLEM

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*Abstract.* In this paper, we give new results on reduction operator algebras. We investigate the relationship between the generalized similarity problem and the total reduction property. We also give some sufficient and necessary conditions for a reduction operator algebra to be self-adjoint or similar to a  $C^*$ -algebra.

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