

## ALGEBRAIC ELEMENTS AND INVARIANT SUBSPACES

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*Abstract.* We prove that if a completely non-unitary contraction  $T$  in  $L(H)$  has a non-trivial algebraic element  $h$ , then  $T$  has a non-trivial invariant subspace.

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