

AUTOMORPHISMS OF $K(H)$ WITH RESPECT TO THE STAR PARTIAL ORDER

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Abstract. Let H be a separable infinite dimensional complex Hilbert space, and let $K(H)$ be the set of all compact bounded linear operators on H . In the paper we characterize the bijective, additive, continuous maps on $K(H)$ which preserve the star partial order in both directions.

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