

THE SIMILARITY DEGREE OF APPROXIMATELY DIVISIBLE C^* -ALGEBRAS

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Abstract. Let \mathcal{A} be a unital approximately divisible C^* -algebra. We show that the similarity degree of \mathcal{A} is at most 5.

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