

DUALITY PROBLEM FOR THE CLASS OF LIMITED COMPLETELY CONTINUOUS OPERATORS

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Abstract. We establish necessary and sufficient conditions under which the class $L_{cc}(E, F)$ of limited completely continuous operators between two Banach lattices verifies the direct and reciprocal duality property.

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