

THE SHILOV BOUNDARY FOR A q -ANALOG OF THE HOLOMORPHIC FUNCTIONS ON THE UNIT BALL OF 2×2 SYMMETRIC MATRICES

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Abstract. We describe the Shilov boundary for a q -analog of the algebra of holomorphic functions on the unit ball in the space of symmetric 2×2 matrices.

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