

## PROPAGATION PHENOMENA FOR MONO-WEAKLY HYPONORMAL OPERATOR PAIRS

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*Abstract.* In this note, we strengthen some of flatness results for mono-polynomially hyponormal and mono-weakly 2-hyponormal 2-variable weighted shifts in [15, 16, 17].

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