

ALGEBRA-VALUED G-FRAMES IN HILBERT C^* -MODULES

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Abstract. In this paper, we consider the notion of algebra-valued G-frame as a special case of G-frame in a Hilbert C^* -module. It is shown that every Hilbert module over a commutative C^* -algebra A admits an algebra-valued G-frame iff A is a C^* -algebra of compact operators.

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