

NUMERICAL RADIUS INEQUALITIES RELATED TO THE GEOMETRIC MEANS OF NEGATIVE POWER

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Abstract. The norm inequalities related to the geometric means are discussed by many researchers. We discuss numerical radius inequalities related to the geometric means. Though the operator norm is unitarily invariant one, the numerical radius is not so and unitarily similar. In this paper, we show numerical radius inequalities related to the geometric means of negative power for positive invertible operators.

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