

## CHARACTERIZATION OF SOME CLASSES OF COMPACT AND MATRIX OPERATORS ON THE SEQUENCE SPACES OF CESÀRO MEANS

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**Abstract.** In this study, we give characterization of the matrix classes  $(|C_{-1}|_k, X)$ , where the spaces  $|C_{-1}|_k, k \geq 1$  have been defined and studied by Hazar and Sarigöl in [15] and  $X = \{c_0, c, \ell_\infty\}$ . Also, we determine the Hausdorff measures of noncompactness of certain matrix operators on the spaces  $|C_{-1}|_k$  and apply our results to characterize some classes of compact operators on those spaces. So, we extend some well known results.

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